

**1.13** The voltage of an electromagnetic wave traveling on a transmission line is given by  $v(z, t) = 5e^{-\alpha z} \sin(4\pi \times 10^9 t - 20\pi z)$  (V), where  $z$  is the distance in meters from the generator.

(a) Find the frequency, wavelength, and phase velocity of the wave.

(b) At  $z = 2$  m, the amplitude of the wave was measured to be 2 V. Find  $\alpha$ .

**Solution:**

(a) This equation is similar to that of Eq. (1.28) with  $\omega = 4\pi \times 10^9$  rad/s and  $\beta = 20\pi$  rad/m. From Eq. (1.29a),  $f = \omega/2\pi = 2 \times 10^9$  Hz = 2 GHz; from Eq. (1.29b),  $\lambda = 2\pi/\beta = 0.1$  m. From Eq. (1.30),

$$u_p = \omega/\beta = 2 \times 10^8 \text{ m/s.}$$

(b) Using just the amplitude of the wave,

$$2 = 5 \exp -\alpha 2, \quad \alpha = \frac{-1}{2 \text{ m}} \ln \left( \frac{2}{5} \right) = 0.46 \text{ Np/m.}$$

---