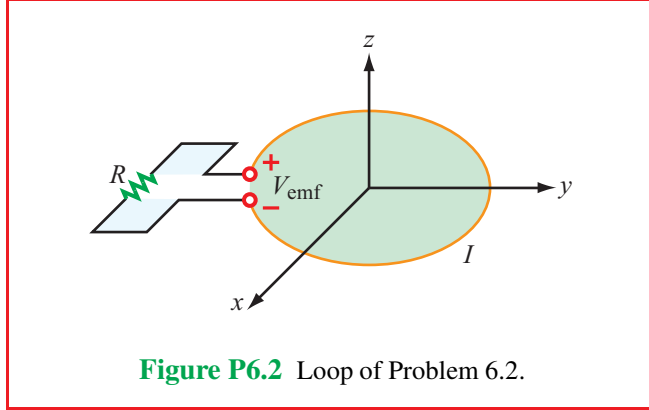


6.2 The loop in Fig. P6.2 is in the x - y plane and $\mathbf{B} = \hat{\mathbf{z}}B_0 \sin \omega t$ with B_0 positive. What is the direction of I ($\hat{\phi}$ or $-\hat{\phi}$) at:

- (a) $t = 0$
- (b) $\omega t = \pi/4$
- (c) $\omega t = \pi/2$



Solution: $I = V_{\text{emf}}/R$. Since the single-turn loop is not moving or changing shape with time, $V_{\text{emf}}^{\text{m}} = 0$ V and $V_{\text{emf}} = V_{\text{emf}}^{\text{tr}}$. Therefore, from Eq. (6.8),

$$I = V_{\text{emf}}^{\text{tr}}/R = \frac{-1}{R} \int_S \frac{\partial \vec{B}}{\partial t} \cdot d\vec{s}.$$

If we take the surface normal to be $+\hat{\mathbf{z}}$, then the right hand rule gives positive flowing current to be in the $+\hat{\phi}$ direction.

$$I = \frac{-A}{R} \frac{\partial}{\partial t} B_0 \sin \omega t = \frac{-AB_0\omega}{R} \cos \omega t \quad (\text{A}),$$

where A is the area of the loop.

(a) A , ω and R are positive quantities. At $t = 0$, $\cos \omega t = 1$ so $I < 0$ and the current is flowing in the $-\hat{\phi}$ direction (so as to produce an induced magnetic field that opposes \mathbf{B}).

(b) At $\omega t = \pi/4$, $\cos \omega t = \sqrt{2}/2$ so $I < 0$ and the current is still flowing in the $-\hat{\phi}$ direction.

(c) At $\omega t = \pi/2$, $\cos \omega t = 0$ so $I = 0$. There is no current flowing in either direction.