2.5 For a parallel-plate transmission line, the line parameters are given by:

$$\begin{aligned} R' &= 2 \qquad (\Omega/\text{m}), \\ L' &= 335 \qquad (\text{nH/m}), \\ G' &= 0, \\ C' &= 344 \qquad (\text{pF/m}). \end{aligned}$$

Find α, β, u_p, and Z_0 at 1 GHz.

Solution: At 1 GHz, $\omega = 2\pi f = 2\pi \times 10^9$ rad/s. Application of (2.22) gives:

$$\begin{aligned} \gamma &= \sqrt{(R' + j\omega L')(G' + j\omega C')} \\ &= [(2 + j2\pi \times 10^9 \times 335 \times 10^{-9})(0 + j2\pi \times 10^9 \times 344 \times 10^{-12})]^{1/2} \\ &= [(2 + j2100)(j2.2)]^{1/2} \\ &= 48e^{j89.97^\circ} = 0.023 + j48. \end{aligned}$$

Hence,

$$\begin{aligned} \alpha &= 0.023 \text{ Np/m}, \\ \beta &= 48 \text{ rad/m}. \end{aligned}$$

$$u_p = \frac{\omega}{\beta} = \frac{2\pi f}{\beta} = \frac{2\pi \times 10^9}{48} = 1.31 \times 10^8 \text{ m/s}.$$

$$\begin{aligned} Z_0 &= \left[\frac{R' + j\omega L'}{G' + j\omega C'}\right]^{1/2} \\ &= \left[\frac{2100e^{j89.95^\circ}}{2.2e^{j90^\circ}}\right]^{1/2} \\ &= \left[954e^{-j0.05^\circ}\right]^{1/2} \\ &= 31e^{-j0.025^\circ} \approx (31 - j0.01)\ \Omega. \end{aligned}$$